

## **WTCS Repository**

# 10-804-197 College Algebra & Trig w Apps

## **Course Outcome Summary**

## **Course Information**

**Description** This course covers skills needed for success in Calculus and many application areas at the baccalaureate level. Algebra topics include the real and complex number systems, polynomials, exponents, radicals, solving equations and inequalities, relations and functions, systems of equations and inequalities, graphing, and conic sections. Trigonometry topics include the unit circle, trigonometric functions, graphs, identities, equations, inverse functions, solutions of triangles, complex numbers, polar coordinates, and vectors.

Total Credits

## **Course History**

Last Revision 5/7/2021 Date

5

#### **Pre/Corequisites**

Prerequisite Each Wisconsin Technical College determines the General Education course prerequisites used by their academic institution. If prerequisites for a course are determined to be appropriate, the final Course Outcome Summary must identify the prerequisites approved for use by the individual Technical College.

## **Course Competencies**

## 1. Analyze the features of a graph of a given function or relation

#### **Assessment Strategies**

1.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

You will know you are successful when you:

- 1.1. differentiate between symmetry about the x-axis, the y-axis, and the origin
- 1.2. determine the domain and range of a relation or function
- 1.3. determine the inverse function of a 1-1 function
- 1.4. specify the relation between the domain and the range of a function and its inverse
- 1.5. apply basic transformations to the elementary functions
- 1.6. differentiate among elementary functions

#### 2. Solve linear and quadratic equations and inequalities

#### **Assessment Strategies**

2.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

Your performance will be successful when you:

- 2.1. relate the solution of an equation to the x-intercept of a graph of the function and to the root (or zero) of the function
- 2.2. use appropriate notation when writing solutions of inequalities
- 2.3. solve quadratic equations using more than one method
- 2.4. use modeling techniques to solve applied problems

#### 3. Analyze the properties of linear and quadratic functions

#### **Assessment Strategies**

3.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

Your performance will be successful when you:

- 3.1. graph quadratic functions
- 3.2. determine the composition of two functions
- 3.3. create new functions by using function operations
- 3.4. apply transformations as compositions of functions
- 3.5. determine the characteristics of a quadratic function
- 3.6. find zeros of quadratic functions algebraically and graphically
- 3.7. convert between standard and vertex form of a quadratic function

#### 4. Analyze polynomials

#### **Assessment Strategies**

4.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

Your performance will be successful when you:

- 4.1. find zeros of polynomial functions
- 4.2. determine whether a function is increasing or decreasing on an interval.
- 4.3. determine the end-behavior of a polynomial function.
- 4.4. use graphical methods to estimate the roots of a polynomial equation.
- 4.5. identify local and global extrema
- 4.6. apply the intermediate value theorem
- 4.7. determine the number of roots of a polynomial equation using the fundamental theorem of algebra.
- 4.8. determine the number of roots of a polynomial function using the fundamental theorem of algebra.
- 4.9. determine all solutions to polynomial equations including complex solutions

#### 5. Analyze rational functions

#### **Assessment Strategies**

5.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

Your performance will be successful when you:

- 5.1. identify removable discontinuities
- 5.2. graph rational functions
- 5.3. perform arithmetic operations with rational expressions
- 5.4. determine the domain of rational functions
- 5.5. determine all asymptotes
- 5.6. solve rational equations

#### 6. Analyze radical functions

#### **Assessment Strategies**

6.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

Your performance will be successful when you:

6.1. solve radical equations

- 6.2. graph radical functions
- 6.3. verify solutions to identify extraneous roots
- 6.4. determine the domain of radical expression

#### 7. Analyze exponential and logarithmic functions

#### **Assessment Strategies**

7.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

You will know you are successful when you:

- 7.1. define the exponential function with an arbitrary base
- 7.2. graph an exponential function with an arbitrary base
- 7.3. model exponential functions to real life applications
- 7.4. solve exponential equations
- 7.5. define logarithmic functions with an arbitrary base
- 7.6. identify the inverse relationship between the logarithmic function and the exponential function
- 7.7. graph a logarithmic function with an arbitrary base
- 7.8. solve logarithmic equations

#### 8. Solve algebraic systems

#### **Assessment Strategies**

8.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

You will know you are successful when you:

- 8.1. solve nonlinear systems of equations
- 8.2. solve systems of linear equations in three or more variables
- 8.3. use systems of three equations to solve applied problems
- 8.4. graph systems of linear inequalities
- 8.5. graph systems of nonlinear equations

#### 9. Analyze conic sections

#### Assessment Strategies

9.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

You will know you are successful when you:

- 9.1. identify all conic sections based on a graph
- 9.2. identify all conic sections based on an equation
- 9.3. analyze the characteristics of all conic sections
- 9.4. sketch the graph of all conic sections given their equations

#### 10. Analyze trigonometric functions

#### **Assessment Strategies**

10.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

#### Your performance will be successful when you:

- 10.1. graph angles in standard position given degree measure
- 10.2. solve problems involving special right triangles
- 10.3. use reference angles to find exact values of trigonometric functions in any quadrant
- 10.4. find the exact value of a trigonometric function given a point on the terminal side of an angle
- 10.5. find the exact value of a trigonometric function given a right triangle
- 10.6. use reciprocal identities
- 10.7. use quotient identities
- 10.8. use Pythagorean identities
- 10.9. use even-odd identities
- 10.10. use cofunction identities

## 11. Evaluate the trigonometric functions

Assessment Strategies

11.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

You will know you are successful when you:

- 11.1. identify exact values of trigonometric functions
- 11.2. find approximate values of trigonometric functions using a calculator
- 11.3. solve right triangles using inverse trigonometric functions
- 11.4. solve right triangles using trigonometric functions

### 12. Apply the unit circle and radian measure

#### **Assessment Strategies**

12.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

You will know you are successful when you:

- 12.1. use the concept of a reference angle
- 12.2. graph angles in standard position given radian measure
- 12.3. relate radian measures to real numbers
- 12.4. convert between radian measures and degree measures of angles
- 12.5. find exact and approximate values of trigonometric functions given in radian measure
- 12.6. analyze the unit circle

## 13. Analyze graphs of trigonometric functions

#### **Assessment Strategies**

13.1. Oral, Written, Graphic and/or Skill Assessment

#### Criteria

## You will know you are successful when you:

- 13.1. sketch graphs of basic trigonometric functions
- 13.2. apply transformations to the graphs of trigonometric functions
- 13.3. identify domains and ranges given trigonometric functions
- 13.4. identify domains and ranges given graphs of trigonometric functions
- 13.5. find equations from graphs of trigonometric functions

## 14. Analyze inverse trigonometric functions

#### **Assessment Strategies**

14.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

You will know you are successful when you:

- 14.1. define the inverse trigonometric functions
- 14.2. identify domains and ranges of inverse trigonometric functions
- 14.3. evaluate the inverse trigonometric functions
- 14.4. evaluate the composition of trigonometric and inverse trigonometric functions

## 15. Manipulate trigonometric identities

#### **Assessment Strategies**

15.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

You will know you are successful when you:

- 15.1. use identities to evaluate trigonometric functions
- 15.2. use trigonometric identities to verify other identities
- 15.3. apply sum and difference identities

- 15.4. apply double-angle and half-angle identities
- 15.5. apply sum-to-product and product-to-sum identities

#### 16. Solve trigonometric equations

#### **Assessment Strategies**

16.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

Your performance will be successful when you:

- 16.1. solve equations involving trigonometric expressions of a single angle
- 16.2. solve equations involving trigonometric expressions of multiple angles
- 16.3. use correct notation to express infinite and finite solution sets of trigonometric equations

#### 17. Solve oblique triangles

**Assessment Strategies** 

17.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

You will know you are successful when you:

- 17.1. use the Law of Sines to solve oblique triangles
- 17.2. use the Law of Cosines to solve oblique triangles
- 17.3. solve application problems involving oblique triangles

#### 18. Complete vector operations

**Assessment Strategies** 

18.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

You will know you are successful when you:

- 18.1. define a vector
- 18.2. define unit vectors i and j
- 18.3. identify the horizontal and vertical components of a vector
- 18.4. find the magnitude of a vector
- 18.5. find the direction of a vector
- 18.6. perform vector addition
- 18.7. perform scalar multiplication of vectors
- 18.8. compute dot product of vectors
- 18.9. determine if two vectors are perpendicular
- 18.10. find the angle measure between two vectors

#### 19. Complete operations with complex numbers in trigonometric form

#### **Assessment Strategies**

19.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

Your performance will be successful when you:

- 19.1. convert complex numbers between rectangular form and trigonometric form
- 19.2. graph complex numbers in trigonometric form and rectangular form
- 19.3. find products of complex numbers written in trigonometric form
- 19.4. find quotients of complex numbers written in trigonometric form

#### 20. Analyze the polar coordinate system

#### **Assessment Strategies**

20.1. Oral, Written, Graphic and/or Skill Assessment

Criteria

Your performance will be successful when you:

- 20.1. 20.2.
- identify points in the polar coordinate system translate between rectangular coordinates and polar coordinates for a given point convert an equation between polar form and rectangular form
- 20.3.
- 20.4. explore graphs of equations in polar form